



NÁRODNÁ BANKA SLOVENSKA  
EUROSYSTEM



# Modelling pension liabilities

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- 1 Definition of pension liabilities**
- 2 Model – concept and features**
- 3 Database and programming code**
- 4 Main assumptions**
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- **Goal**

- **give an overview of pension obligations towards households**
- **standardized table in 2008 SNA/ESA2010**
- **includes the PV of pension entitlements arising from already accrued pension rights**
- **covers every pension type (including old age, survivor's and disability pensions)**
- **reports relations between stocks and flows in schemes**
- **includes defined benefit schemes and defined contributory schemes, private and general government pension schemes**

- **The Role of NBS**

- **modelling pension entitlements (I. pillar - general government, army/police pension schemes)**

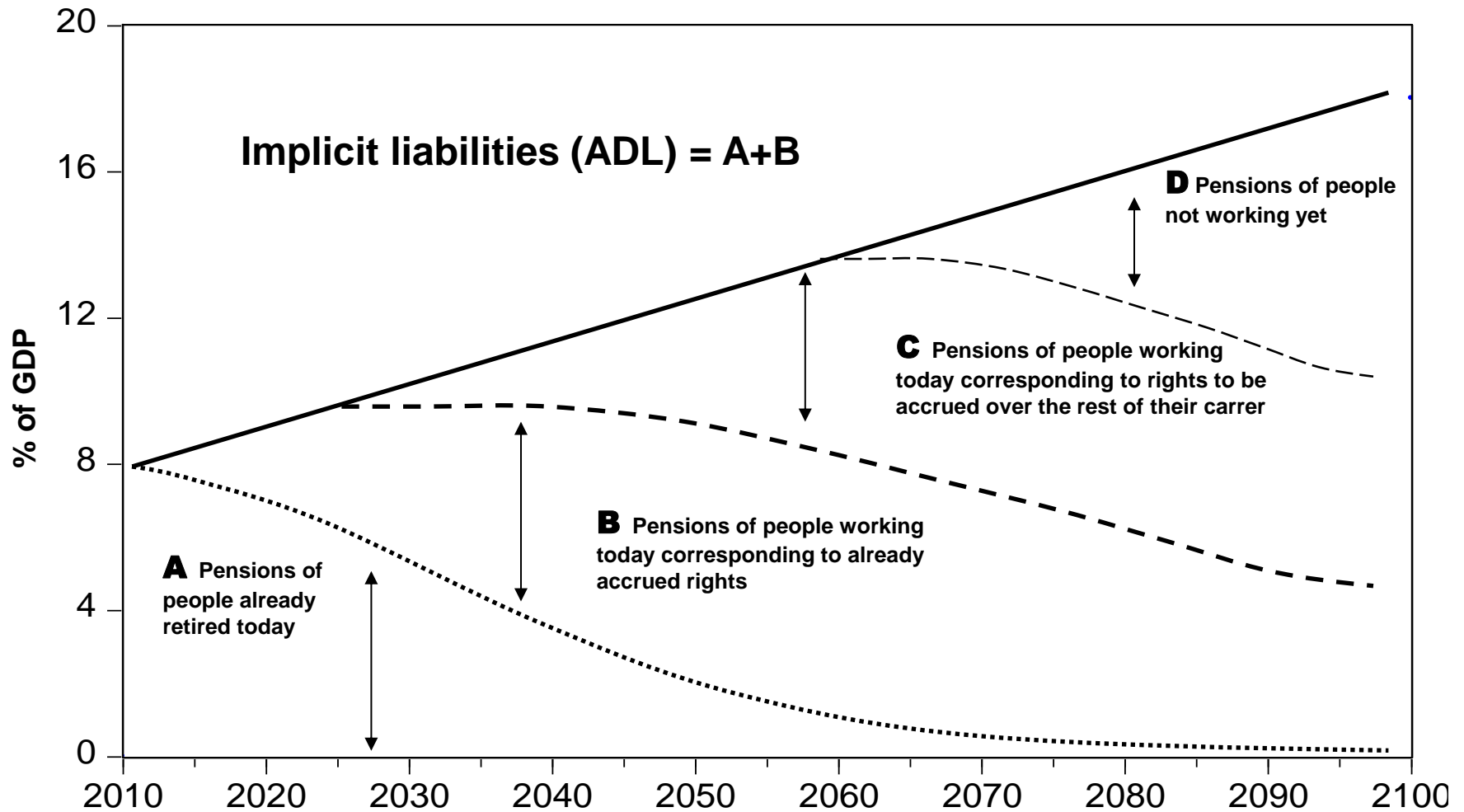
# Supplementary table in ESA2010 (2)



The supplementary table on pension schemes in social insurance

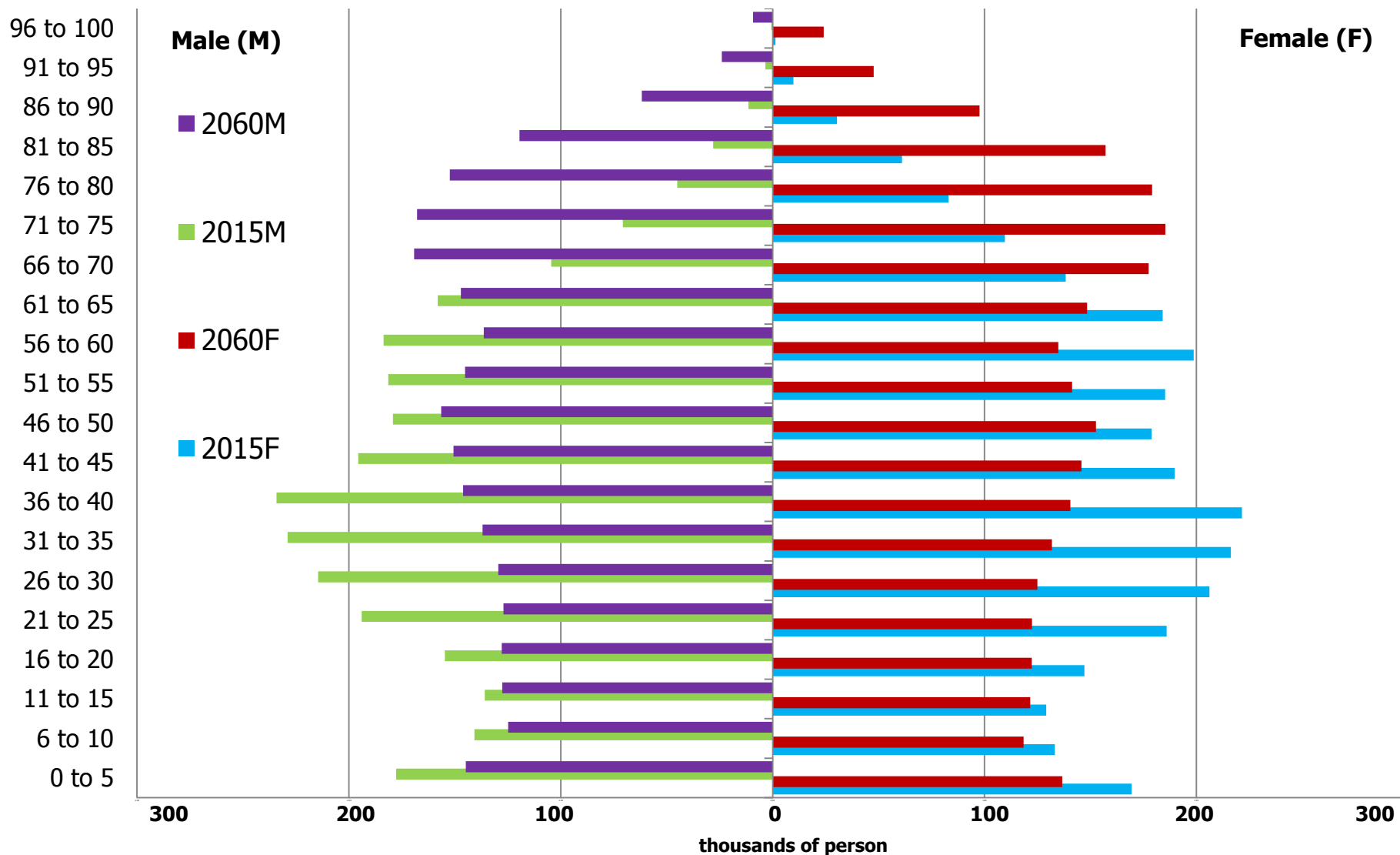
Relations	Row No.	Recording Pension manager	Core national accounts						Not in the core national accounts		Total pension schemes	Counterparts: Pension entitlements of non-resident households <sup>4)</sup>
			Non-general government			General government			Social security pension schemes			
			Defined contribution schemes	Defined benefit schemes and other <sup>1)</sup> non-defined contribution schemes	Total	Defined contribution schemes	Defined benefit schemes for general government employees <sup>2)</sup>					
							Classified in financial corporations	Classified in general govt 3)		Classified in general government		
Column number	A	B	C	D	E	F	G	H	I	J		
			<b>Opening balance sheet</b>									
	1	Pension entitlements										
			<b>Changes in pension entitlements due to transactions</b>									
Σ 2.1 to 2.5	2	Increase in pension entitlements due to social contributions										
	2.1	Employer actual social contributions										
	2.2	Employer imputed social contributions										
	2.3	Household actual social contributions										
	2.4	Household social contribution supplements <sup>5)</sup>										
	2.5	Less: Pension scheme service charges										
	3	Other (actuarial) change of pension entitlements in social security pension schemes										

# Coverage in ESA2010



(Source: Eurostat, ECB, 2010)

# Demographic projection by age groups in Slovakia



source: *Europop 2015*

# Key changes in pension system in Slovakia



- **Introduction of funded II. pillar scheme**
  - has impact on implicit debt in general SS pension scheme
  - 2005-3q2012 social contribution divided between I. (PAYG) and II. pillar, old-age contribution (18% of wage base) divided equally between pillars (9%/9%)
  - 4q2012 -2016 contributions divided into 14%/ 4%
  - gradually in 2017-2024 change of 0,25 points a year to ratio 12%/6%
  - participation in the II. pillar is not mandatory
- **Changes in pension indexation**
  - shift from Wage/Inflation indexation towards Inflation
  - Minimum pension
- **Change in retirement age**
  - generally 62 years (both men and women)
  - after 2017 linked to changes in life expectancy
- **Extended minimum years of service in army/police**
  - from 15 to 25 years (2013)

# Model (1) – composition



- **Liabilities to:**
  - **current contributor**
  - **current pensioner**
- **Entitlements by type:**
  - **old age pensions**
  - **early-old age pensions**
  - **disability pension**
  - **survivor's pension**
- **Pension schemes:**
  - **general government pension scheme**
  - **army social security pension scheme (VUSZ)**
  - **police social security pension scheme (MV SR)**





- **Beneficiaries – calculation:**

- **in the year  $t_0$**
- **for cohort group of age  $x$**
- **gender  $g$**

$$TL_{[g,x]t_0}^B = \sum_{t=1}^{100-x} S_{[g,x],t_0}^B p_{[g,x]t} \frac{\prod_{i=1}^t (1+v_i)}{(1+r)^t}, \quad x \in \langle x_0, 100 \rangle$$

- $S_{[g,x],t_0}^B$  - **sum of pensions paid to  $[g, x]$  in the year  $t_0$**
- $p_{[g,x]t}$  - **survival rate of the year  $x+t$**
- $v_i$  - **valorization rate**
- $r$  - **discount rate**

- **Beneficiaries – total liabilities:**

$$TL_{t_0}^B = \sum_{x=x_0}^{100-1} TL_{[male,x]t_0}^B + \sum_{x=x_0}^{100-1} TL_{[female,x]t_0}^B$$

# Model (3) – estimating pension entitlements



- **Contributors, I. pillar – calculation:**

- **in the year  $t_0$**
- **for cohort group of age  $x$**
- **gender  $g$**

$$TL_{[g,x]t_0}^{C,I} = n_{[g,x]t_0} \lambda_x \alpha_{[g,x]t_0} \sum_{t=1}^{100-x} S_{[g,x],t_0}^C p_{[g,x]t}^O \sum_{s=0}^{100-x-t+1} p_{[g,x]t+s} \frac{\prod_{i=t+1}^{t+s} (1+v_i)}{(1+r)^{t+s}}$$

- $n_{[g,x]t_0}$  - **number of contributors  $[g, x]$  in the year  $t_0$**
- $\lambda_x = (\text{Actual age} - \text{Start contribution}) / (\text{Retirement age} - \text{Start contr.})$
- $\alpha_{[g,x]t_0}$  - **I. pillar contributor's share**
- $S_{[g,x],t_0}^C$  - **annual amount of future pension in cohort  $[g, x]$**
- $p_{[g,x]t}^O$  - **probability of insurance event**
- $p_{[g,x]t+s}$  - **survival rate of the year  $x+t$**
- $v_i$  - **valorization rate,  $r$  – discount rate**



- Contributors, II. pillar – calculation:

- in the year  $t_0$
- for cohort group of age  $x$
- gender  $g$

$$TL_{[g,x]t_0}^{C,II} = n_{[g,x]t_0} \lambda_x (1 - \alpha_{[g,x]t_0}) (1 - \beta_x) \sum_{t=1}^{100-x} S_{[g,x],t_0}^C p_{[g,x]t}^O \sum_{s=0}^{100-x-t+1} p_{[g,x]t+s} \frac{\prod_{i=t+1}^{t+s} (1 + v_i)}{(1 + r)^{t+s}}$$

- $\beta_x$  - II. pillar participation share of contributor's cohort  $[g, x]$

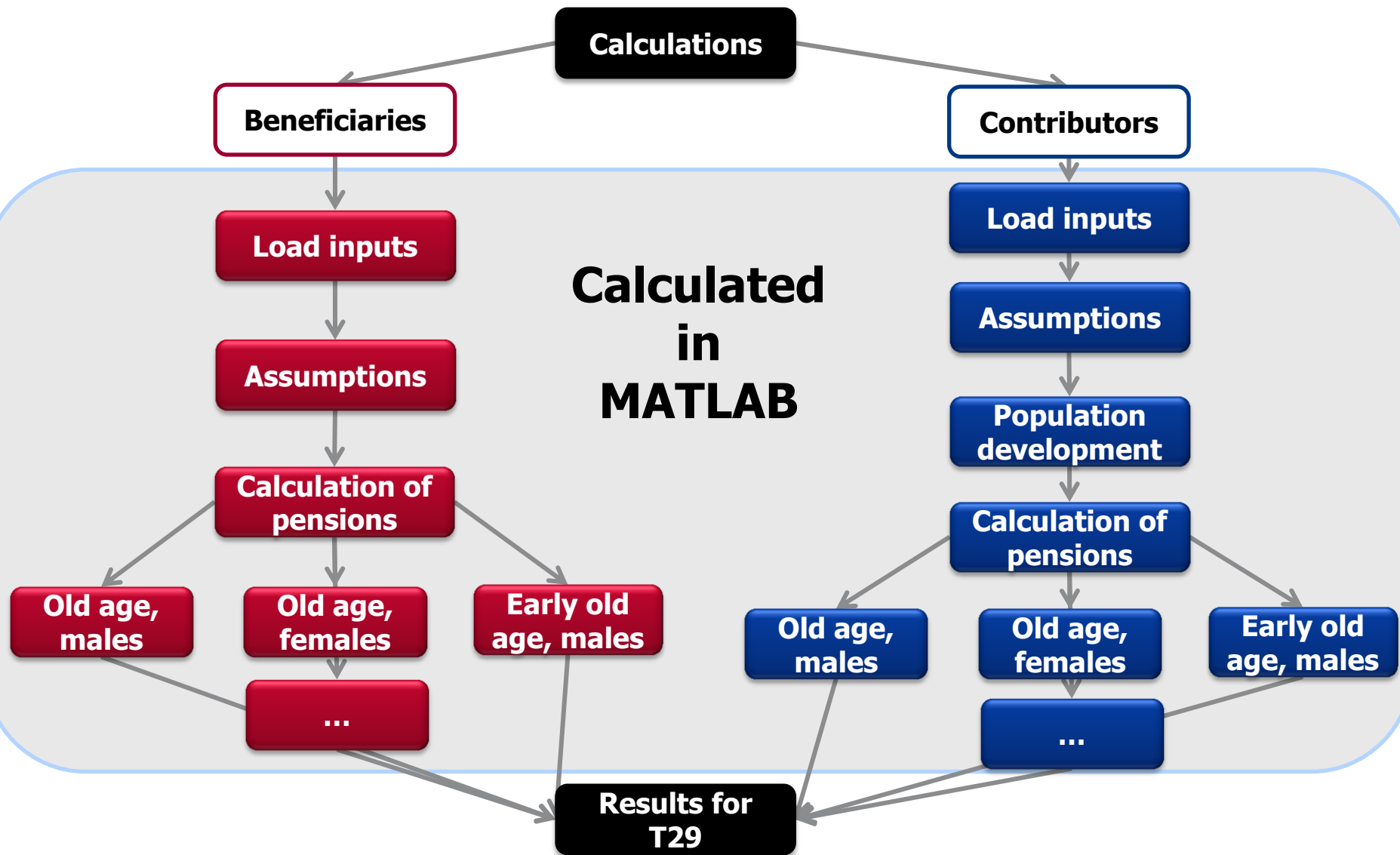
- Contributors – total liabilities:

$$TL_{t_0}^C = \sum_{g \in \{M,F\}} \sum_{x=x_0}^{100-1} TL_{[g,x]t_0}^{C,I} + \sum_{g \in \{M,F\}} \sum_{x=x_0}^{100-1} TL_{[g,x]t_0}^{C,II}$$



- **Social Insurance Agency in Slovakia**
  - **data of current pensioners (numbers, average pensions)**
  - **pension expenditures**
  - **current workers (numbers, average wages)**
  - **II. pillar contributors**
- **Military/Police Social Security Office**
  - **data of current pensioners (numbers, average pensions)**
  - **current military/police forces (numbers, average wages)**
- **Database**
  - **all data in cohorts – divide to the age groups, gender (type of pension – for pensioners)**

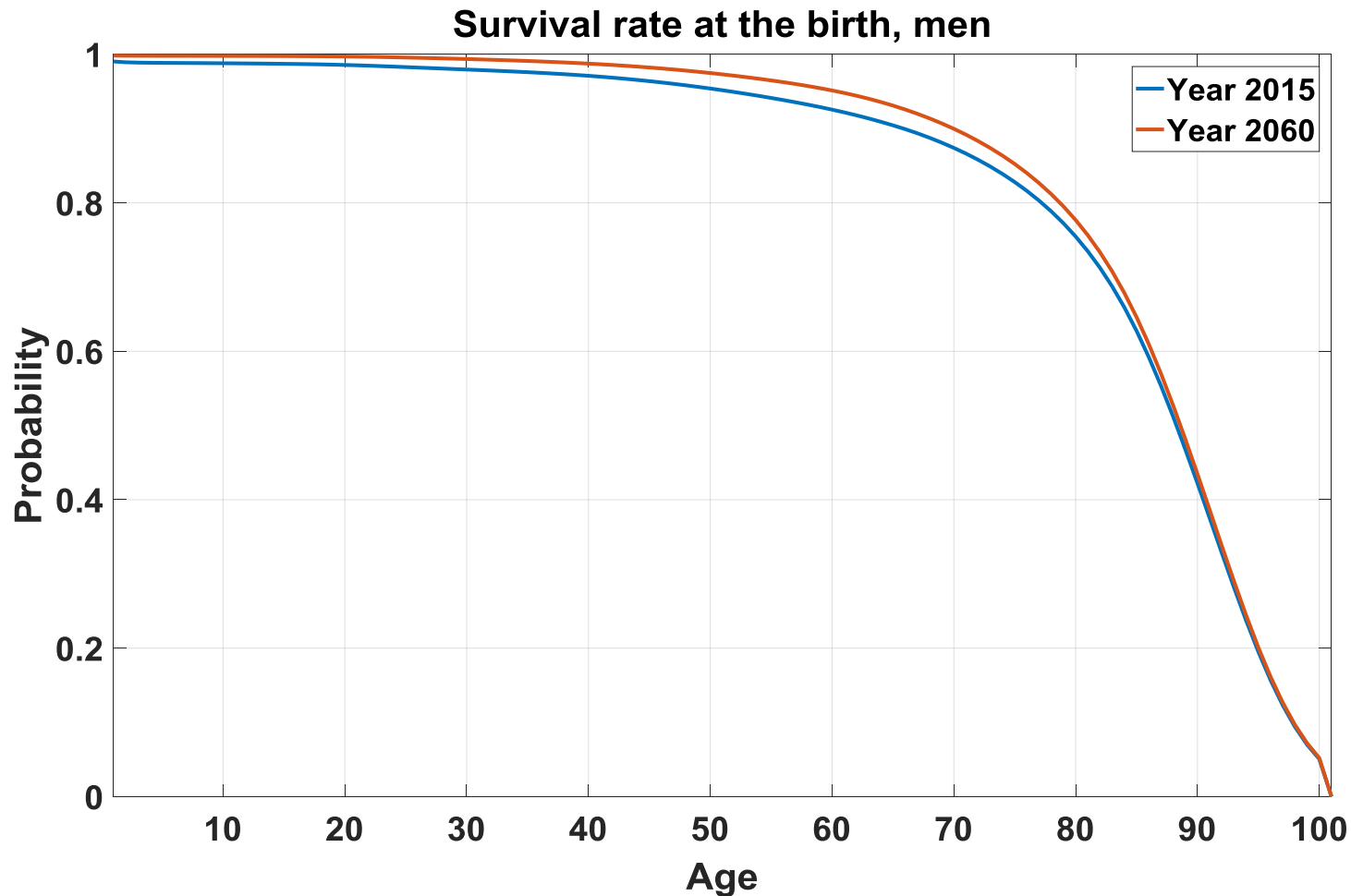
# Programming scheme



# Main assumptions (1)



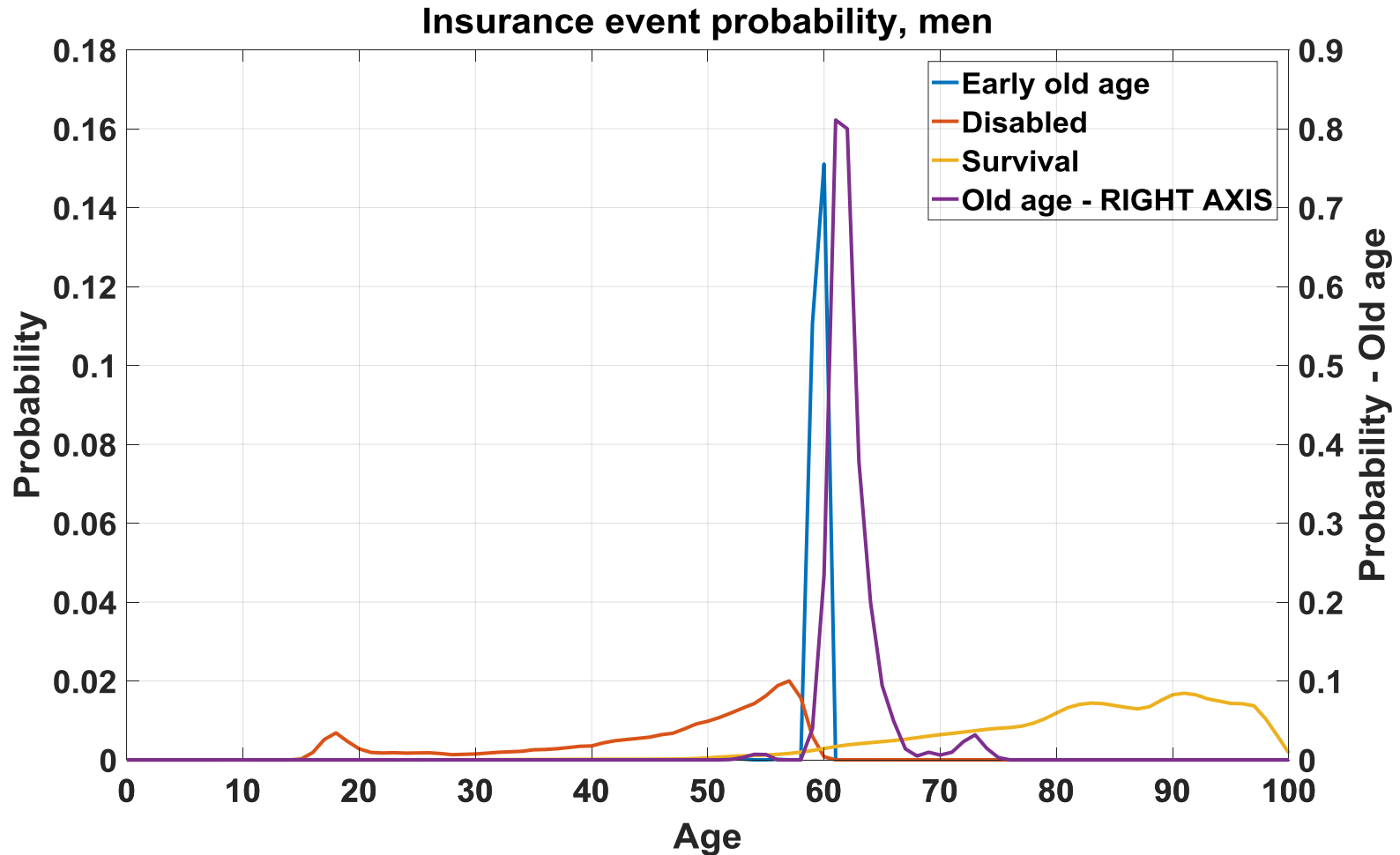
- **Survival rate**
  - **consistent with demographic Europop assumptions**



# Main assumptions (2)



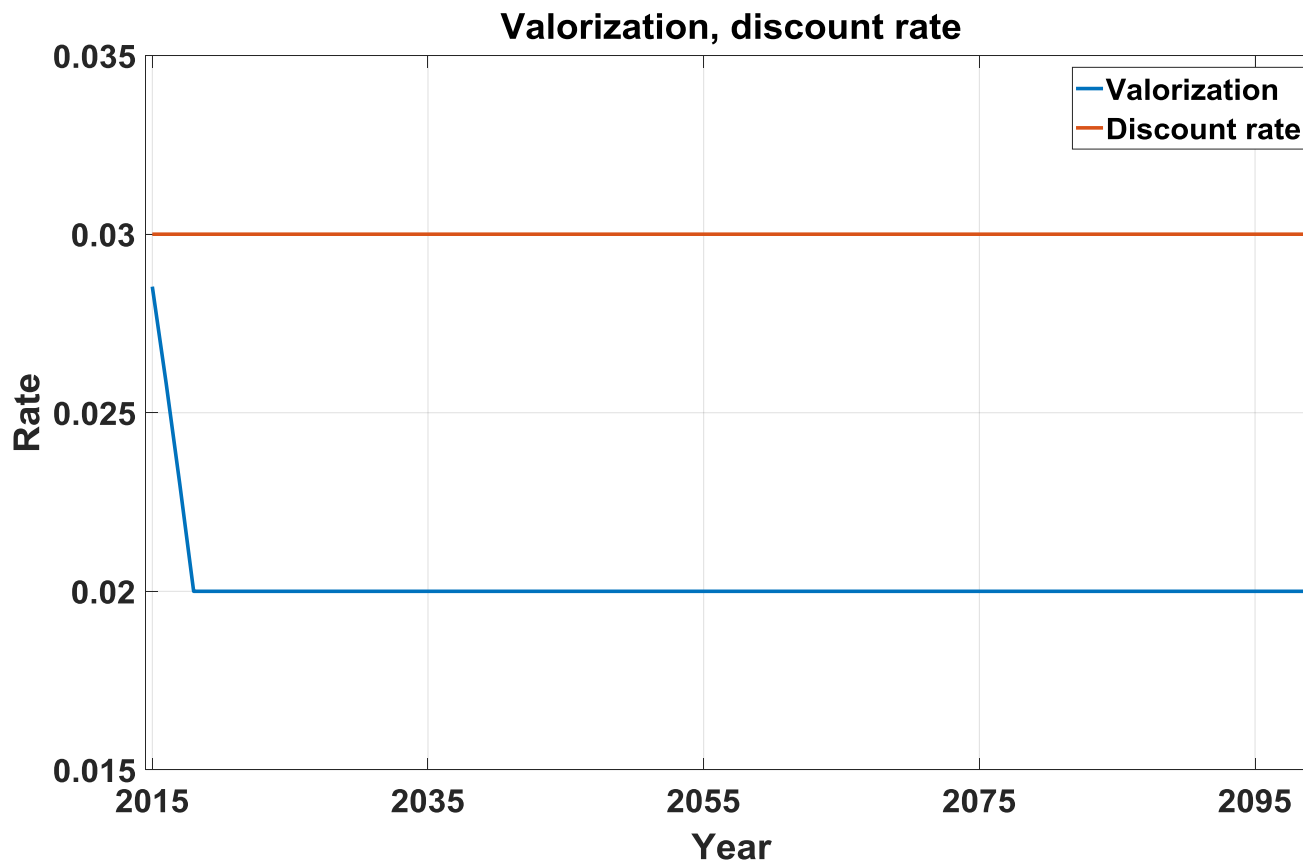
- **Insurance event probability**
  - **computed from data from previous years**
  - **approximation**



# Main assumptions (3)



- **Pension valorization**
  - **legislation based**
  - **in Slovakia – wage → inflation growth dependent**
  - **inflation – 2% - according to Eurostat Technical guide**
- **Discount rate**
  - **3% - according to Eurostat Technical guide**

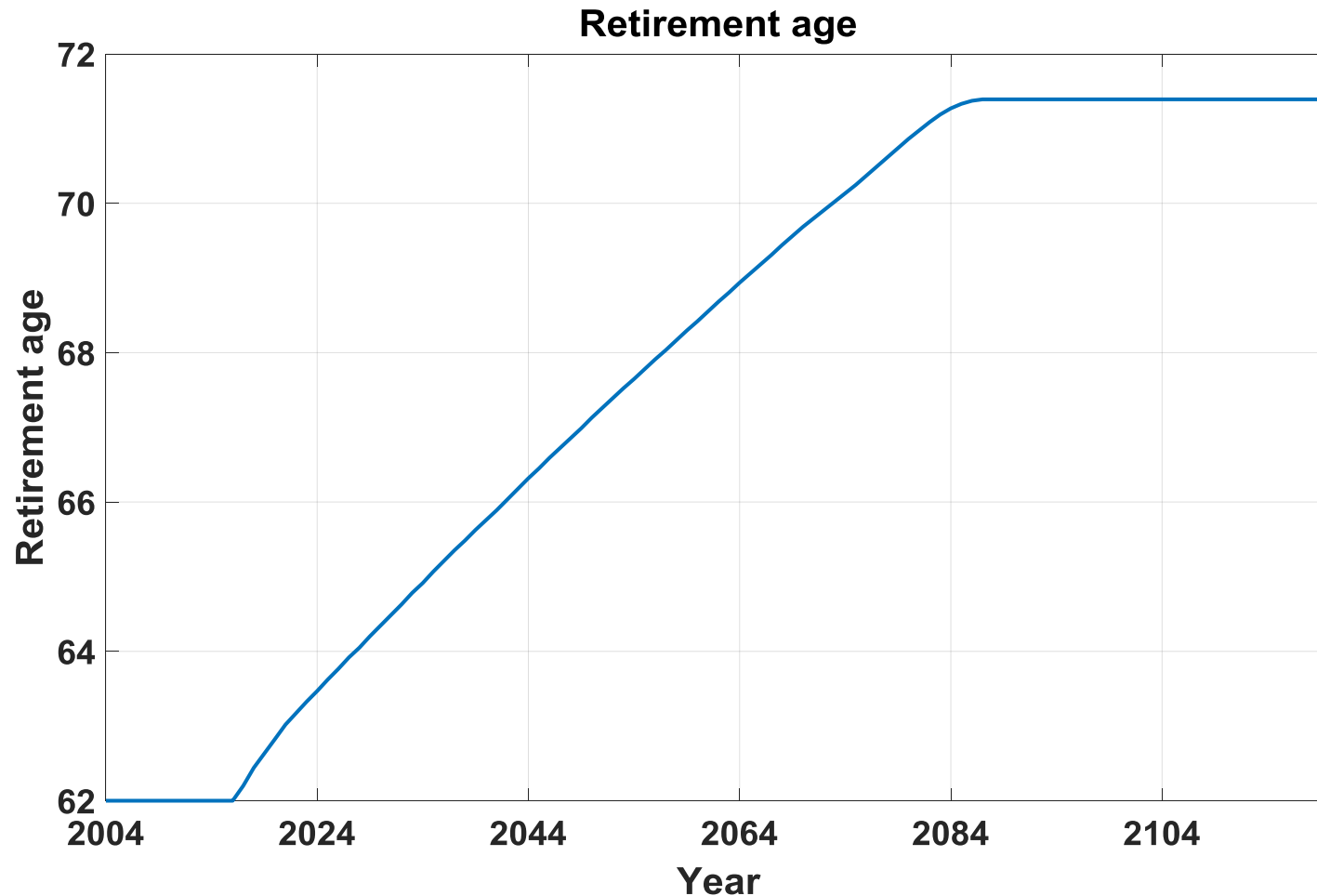




# Main assumptions (6)



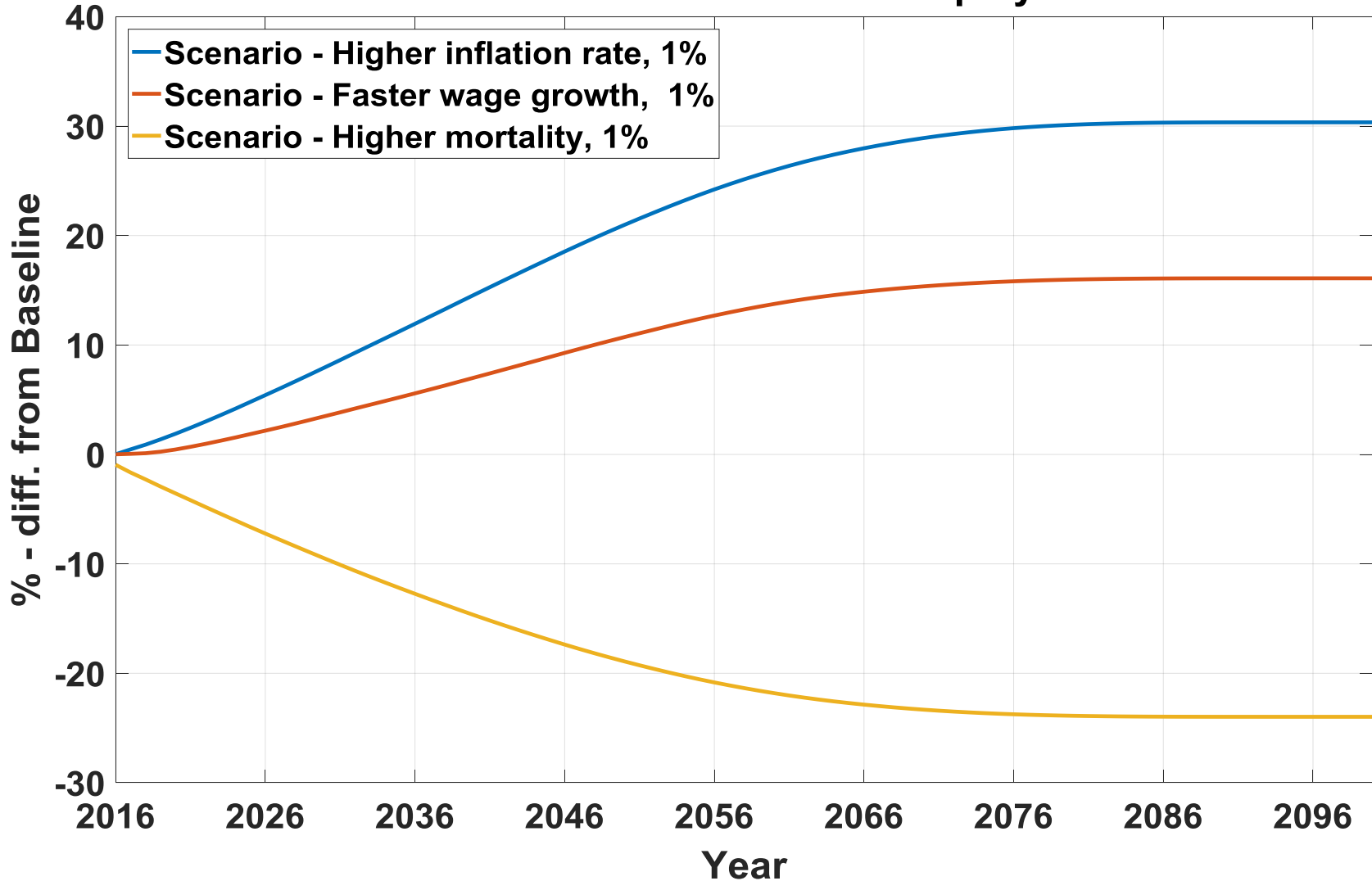
- **Retirement age**
  - **legislation based**
  - **fixed to the life expectancy at retirement age**



# Simulation results



## Liabilities to contributors - employees



# Conclusion



- **Done (small improvements to be added)**
  - **calculation for general government pension scheme**
  - **evaluation scenarios**
- **In progress**
  - **Evaluation calculation liabilities for army social security system**
  - **Evaluation calculation liabilities for police social security system**
- **Next**
  - **Discuss possible scenarios of main assumptions (mainly about insurance event probability)**
  - **Compare results with other countries**



# Thank you

## References

- **European Commission**, The 2015 Ageing Report: Underlying Assumptions and Projection Methodologies, 2014, Brussels
- **Eurostat, ECB**, Eurostat Population projection Europop 2015, [http://ec.europa.eu/eurostat/data/database?node\\_code=proj](http://ec.europa.eu/eurostat/data/database?node_code=proj), 2017
- **Eurostat, ECB**, Technical Compilation Guide for Pension Data in National Accounts, 2011 edition, Luxembourg
- **Statistics Netherlands**, Constructing the Supplementary Pension Table for the Netherlands, 2015/07